

UNIDAD 2: ECUACIONES Y SISTEMAS

ECUACIONES

1. $\frac{x+4}{3} - \frac{7-x}{x-3} = \frac{4x+7}{9} - 1$

$x_1=21, x_2=5$

2. $2x^4 - 3x^2 - 20 = 0$

$x_1 = -2, x_2 = 2$

3. $x^6 - 19x^3 = 216$

$x_1 = 3, x_2 = -2$

4. $\left(x+1+\frac{6}{x}\right) \cdot \left(x-1+\frac{6}{x}\right) = 24$

$x_1 = 3, x_2 = -3, x_3 = 2, x_4 = -2$

5. $2x^3 - \sqrt{x^3} = 120$

$x_1 = 4$

6. $x^8 - x^4 - 240 = 0$

$x_1 = -2, x_2 = 2$

7. $\sqrt{x^2 + x + 4} = 2 + \sqrt{x^2 - 2x + 1}$

$x_1 = 3, x_2 = 5/7$

8. $\frac{x^2 - 32}{4} + \frac{28}{x^2 - 9} = 0$

$x_1 = 5, x_2 = -5, x_3 = 4, x_4 = -4$

9. $\sqrt{3x+1} - \sqrt{2x-1} = 1$

$x_1 = 1, x_2 = 5$

10. $\sqrt{9+x} - 5 = \frac{2x+1}{3}$

$x = -5$

11. $4^{x+1} + 2^{x+3} - 320 = 0$

$x = 3$

12. $3^{2(x+1)} - 28 \cdot 3^x + 3 = 0$

$x_1 = 1, x_2 = -2$

13. $2^{2x} + 2^{2x-1} + 2^{2(x-1)} + 2^{2x-3} + 2^{2(x-2)} = 1984$

$x = 5$

14. $2^{x-1} + 2^{x-2} + 2^{x-3} + 2^{x-4} = 960$

$x = 10$

15. $3^x + 3^{1-x} = 4$

$x_1 = 0, x_2 = 1$

16. $2^{1-x^2} = \frac{1}{8}$

$x_1 = 2, x_2 = -2$

17. $(x^2 - 5x + 9)\lg 2 + \lg 125 = 3$

$x_1 = 2 \text{ y } x_2 = 3$

18. $\lg(2^{2-x})^{2+x} + \lg 1250 = 4$

$x_1 = -1 \text{ y } x_2 = 1$

$$19. \frac{\lg 2 + \lg(11 - x^2)}{\lg(5 - x)} = 2$$

$$x_1=3, x_2=1/3$$

$$20. (x^2 - 4x + 7)\lg 5 + \lg 16 = 4$$

$$x_1=1, x_2=3$$

$$21. 3\lg x - \lg 32 = \lg(x/2)$$

$$x = 4$$

$$22. 5\lg \frac{x}{2} + 2\lg \frac{x}{3} = 3\lg x - \lg \frac{32}{9}$$

$$x = 3$$

$$23. 2\lg x = 3 + \lg(x/10)$$

$$x = 10$$

SISTEMAS

$$24. \begin{cases} x \cdot y = 15 \\ \frac{x}{y} = \frac{5}{3} \end{cases}$$

$$(5, 3), (-5, -3)$$

$$25. \begin{cases} x^2 + y^2 - 5x - 5y = -10 \\ x^2 - y^2 - 5x + 5y = -2 \end{cases}$$

$$(2, 1), (2, 4), (3, 1), (3, 4)$$

$$26. \begin{cases} (x - y)(x + y) = 7 \\ 3x - 4y = 0 \end{cases}$$

$$(4, 3), (-4, -3)$$

$$27. \begin{cases} x + y + z = 2 \\ 2x + 3y + 5z = 11 \\ x - 5y + 6z = 29 \end{cases}$$

$$(1, -2, 3)$$

$$28. \begin{cases} 3x - y + z = 1 \\ x + 2y - 2z = -1 \\ 2x - 3y + z = -1 \end{cases}$$

$$(1/7, 13/14, 3/2)$$

$$29. \begin{cases} x - y = 1 \\ 2x + 6y - 5z = -4 \\ x + y - z = 0 \end{cases}$$

$$(3/2, 1/2, 2)$$

$$30. \begin{cases} x + y + z = 2 \\ -2x + y + 2z = 2 \\ 3x - 2y - z = 4 \end{cases}$$

$$(1, -2, 3)$$